



Laws of logarithms

What a logarithm asks

$\log_2 8 = 3$ What power of 2 makes 8?

$$2^3 = 8$$

$\log 1000$ A bare log is base 10; $\ln$ is base e.

$$= 3, \text{ because } 10^3 = 1000$$

Change of base Divide two logs it has.

$$\log_2 40 = \log 40 \div \log 2$$

The three laws

$\times$ inside Add the logs.

$$\log 4 + \log 25 = \log 100 = 2$$

$\div$ inside Subtract the logs.

$$\log 500 - \log 5 = \log 100 = 2$$

Power inside Bring it out in front.

$$\log_2 8^3 = 3 \times \log_2 8 = 9$$

Expand $\log(x^2y \div z)$ — one law at a time

1 Divide $\rightarrow$ subtract

$$\log(x^2y) - \log z$$

2 Multiply $\rightarrow$ add

$$\log x^2 + \log y - \log z$$

3 Power $\rightarrow$ out in front

$$2 \log x + \log y - \log z$$

Not this — this

$\log(x + y)$ is not $\log x + \log y$.

adding logs multiplies

$\log x \div \log y$ is not $\log(x \div y)$.

that one is $\log x - \log y$

$(\log x)^2$ is not $2 \log x$.

$$2 \log x = \log x^2$$

$\log 1$ is 0, not 1.

any base to the power 0 is 1