

Grade 7 Geometry Workbook

7 lessons · printable · answer key at the back



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book

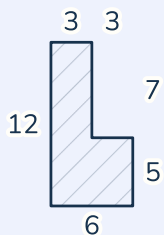
Name _____ Date _____

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Area of Composite Shapes

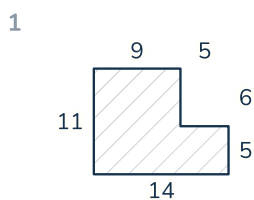
WORKED EXAMPLE



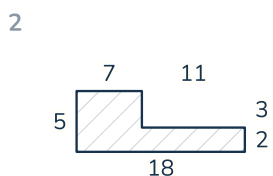
51 cm²

1. Area of composite figures

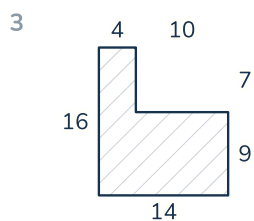
Find the area of each figure. All lengths are in centimeters.



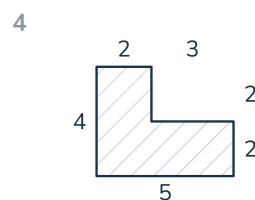
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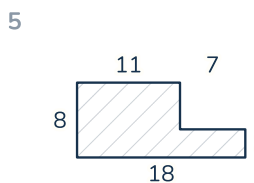
_____ cm²



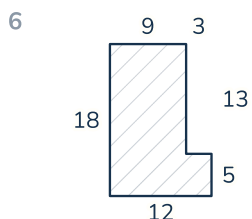
_____ cm²



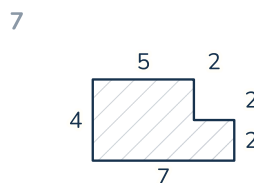
_____ cm²



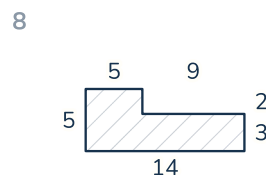
_____ cm²



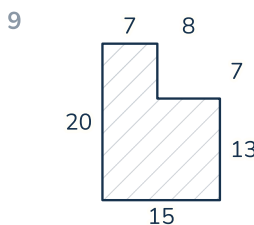
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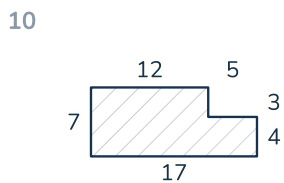
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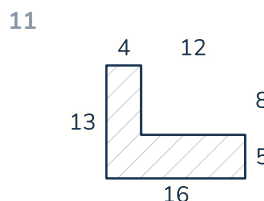
_____ cm²



_____ cm²



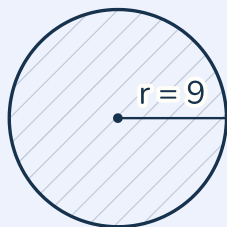
_____ cm²



_____ cm²

Area of a Circle

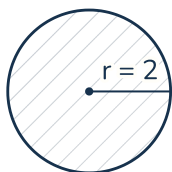
WORKED EXAMPLE


254.34 cm²

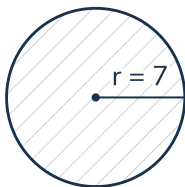
2. Area of a circle

Find the area of each circle. Use $\pi = 3.14$.

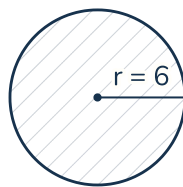
1

_____ cm²

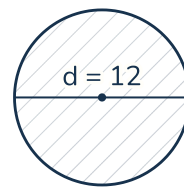
2

_____ cm²

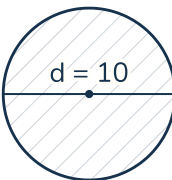
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_____ cm²

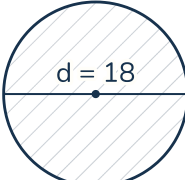
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_____ cm²

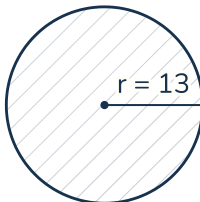
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_____ cm²

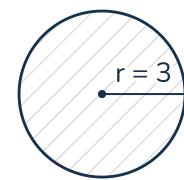
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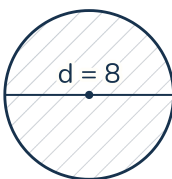
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_____ cm²

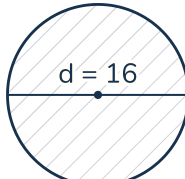
8

_____ cm²

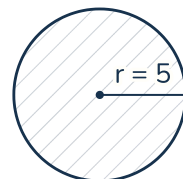
9

_____ cm²

10

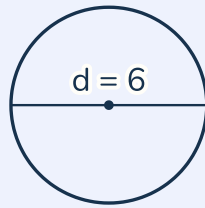
_____ cm²

11

_____ cm²

Circumference

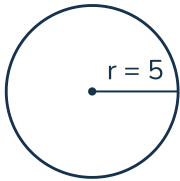
WORKED EXAMPLE

**18.84** cm

3. Circumference of a circle

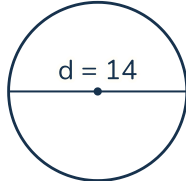
Find the circumference of each circle. Use $\pi = 3.14$.

1



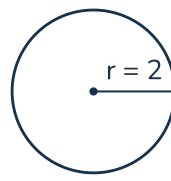
_____ cm

2



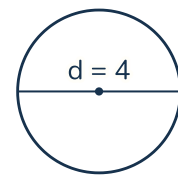
_____ cm

3



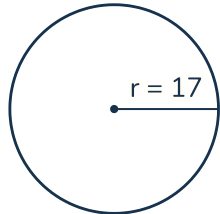
_____ cm

4



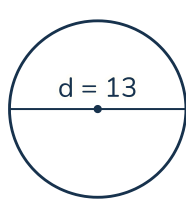
_____ cm

5



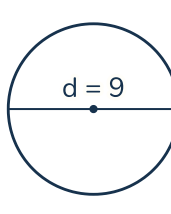
_____ cm

6



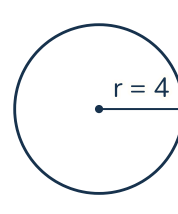
_____ cm

7



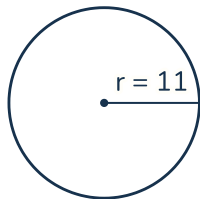
_____ cm

8



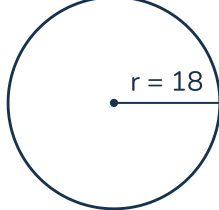
_____ cm

9



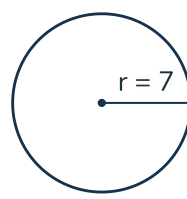
_____ cm

10



_____ cm

11



_____ cm

Angle Pairs

WORKED EXAMPLE



35 degrees

4. Missing angles in a pair

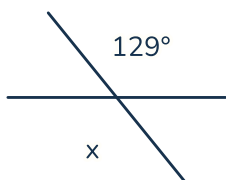
Find the angle marked x . Give each answer in degrees.

1



_____ degrees

2



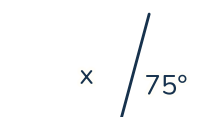
_____ degrees

3



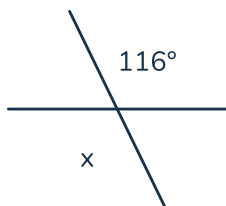
_____ degrees

4



_____ degrees

5



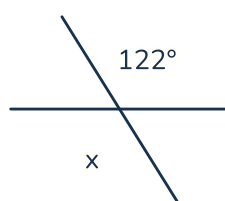
_____ degrees

6



_____ degrees

7



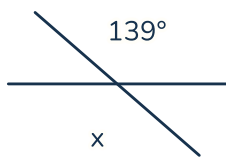
_____ degrees

8



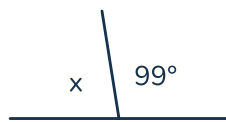
_____ degrees

9



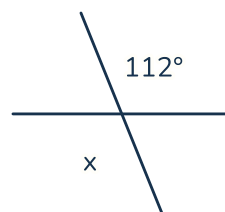
_____ degrees

10



_____ degrees

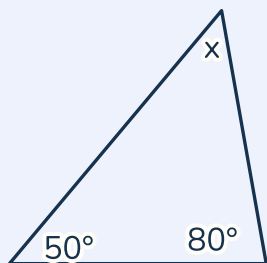
11



_____ degrees

Angles in a Triangle

WORKED EXAMPLE

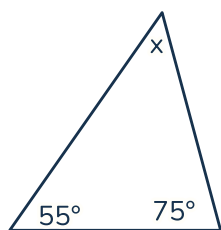


50 degrees

5. The third angle of a triangle

Find the angle marked x . Give each answer in degrees.

1



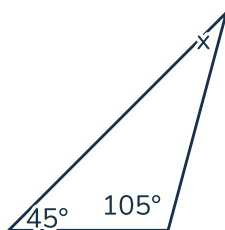
_____ degrees

2



_____ degrees

3



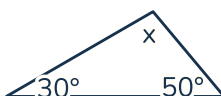
_____ degrees

4



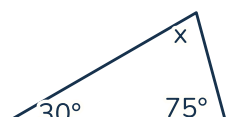
_____ degrees

5



_____ degrees

6



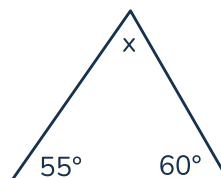
_____ degrees

7



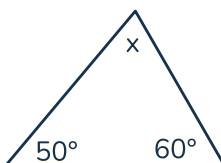
_____ degrees

8



_____ degrees

9



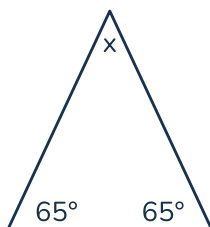
_____ degrees

10



_____ degrees

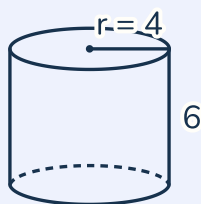
11



_____ degrees

Volume of Cylinders

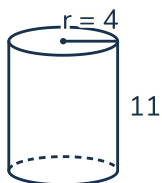
WORKED EXAMPLE

**301.44**

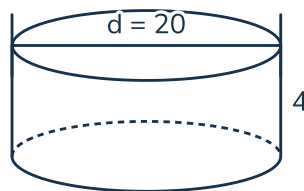
6. Volume of a cylinder

Find the volume of each cylinder. Use $\pi = 3.14$.

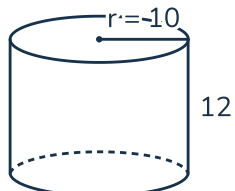
1



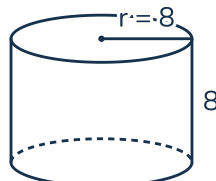
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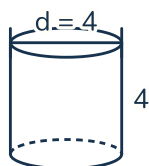
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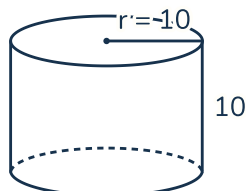
4



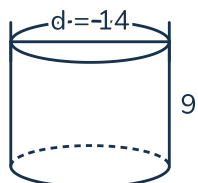
5



6

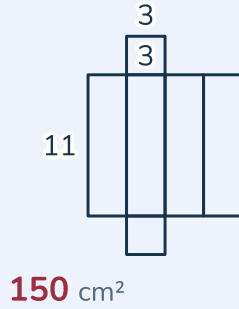


7



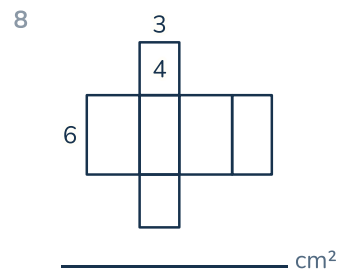
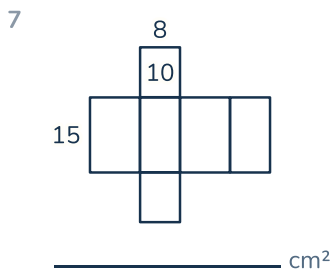
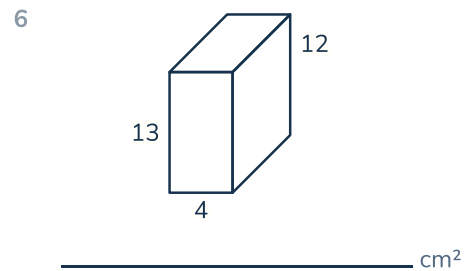
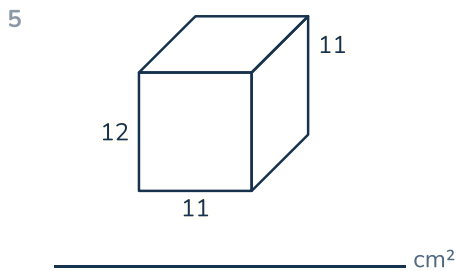
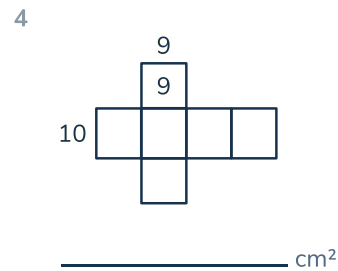
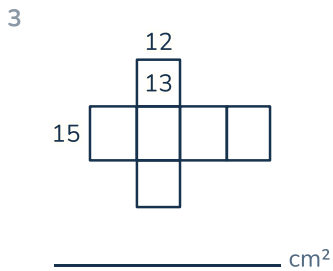
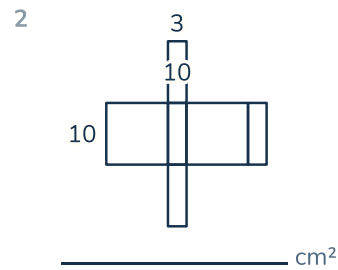
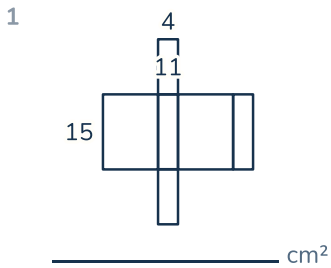
Surface Area

WORKED EXAMPLE



7. Surface area of a box

Find the surface area of each box. All lengths are in centimeters.



Answer Key

Area of Composite Shapes

Area of composite figures

1. 14×11 less 5×6 : 124 cm^2
2. 18×5 less 11×3 : 57 cm^2
3. 14×16 less 10×7 : 154 cm^2
4. 5×4 less 3×2 : 14 cm^2
5. 18×8 less 7×5 : 109 cm^2
6. 12×18 less 3×13 : 177 cm^2
7. 7×4 less 2×2 : 24 cm^2
8. 14×5 less 9×2 : 52 cm^2
9. 15×20 less 8×7 : 244 cm^2
10. 17×7 less 5×3 : 104 cm^2
11. 16×13 less 12×8 : 112 cm^2

Area of a Circle

Area of a circle

1. $r = 2$: 12.56 cm^2
2. $r = 7$: 153.86 cm^2
3. $r = 6$: 113.04 cm^2
4. $d = 12$: 113.04 cm^2
5. $d = 10$: 78.5 cm^2
6. $d = 18$: 254.34 cm^2
7. $r = 13$: 530.66 cm^2
8. $r = 3$: 28.26 cm^2
9. $d = 8$: 50.24 cm^2
10. $d = 16$: 200.96 cm^2
11. $r = 5$: 78.5 cm^2

Circumference

Circumference of a circle

1. $r = 5$: 31.4 cm
2. $d = 14$: 43.96 cm
3. $r = 2$: 12.56 cm
4. $d = 4$: 12.56 cm
5. $r = 17$: 106.76 cm
6. $d = 13$: 40.82 cm
7. $d = 9$: 28.26 cm
8. $r = 4$: 25.12 cm
9. $r = 11$: 69.08 cm
10. $r = 18$: 113.04 cm
11. $r = 7$: 43.96 cm

Angle Pairs

Missing angles in a pair

1. supplementary, 83° : 97°
2. vertical, 129° : 129°
3. supplementary, 97° : 83°

Angle Pairs (continued)

Missing angles in a pair (continued)

4. supplementary, 75° : 105°
5. vertical, 116° : 116°
6. supplementary, 64° : 116°
7. vertical, 122° : 122°
8. complementary, 52° : 38°
9. vertical, 139° : 139°
10. supplementary, 99° : 81°
11. vertical, 112° : 112°

Angles in a Triangle

The third angle of a triangle

1. $55^\circ + 75^\circ = 130^\circ$: 50°
2. $25^\circ + 60^\circ = 85^\circ$: 95°
3. $45^\circ + 105^\circ = 150^\circ$: 30°
4. $75^\circ + 80^\circ = 155^\circ$: 25°
5. $30^\circ + 50^\circ = 80^\circ$: 100°
6. $30^\circ + 75^\circ = 105^\circ$: 75°
7. $30^\circ + 80^\circ = 110^\circ$: 70°
8. $55^\circ + 60^\circ = 115^\circ$: 65°
9. $50^\circ + 60^\circ = 110^\circ$: 70°
10. $25^\circ + 50^\circ = 75^\circ$: 105°
11. $65^\circ + 65^\circ = 130^\circ$: 50°

Volume of Cylinders

Volume of a cylinder

1. $r = 4$, $h = 11$: 552.64 cm^3
2. $d = 20$, $h = 4$: 1256 cm^3
3. $r = 10$, $h = 12$: 3768 cm^3
4. $r = 8$, $h = 8$: 1607.68 cm^3
5. $d = 4$, $h = 4$: 50.24 cm^3
6. $r = 10$, $h = 10$: 3140 cm^3
7. $d = 14$, $h = 9$: 1384.74 cm^3

Surface Area

Surface area of a box

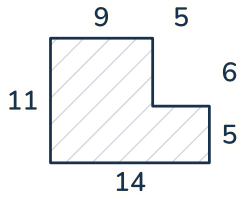
1. $4 \times 11 \times 15 \rightarrow 2(44 + 60 + 165)$: 538 cm^2
2. $3 \times 10 \times 10 \rightarrow 2(30 + 30 + 100)$: 320 cm^2
3. $12 \times 13 \times 15 \rightarrow 2(156 + 180 + 195)$: 1062 cm^2
4. $9 \times 9 \times 10 \rightarrow 2(81 + 90 + 90)$: 522 cm^2
5. $11 \times 11 \times 12 \rightarrow 2(121 + 132 + 132)$: 770 cm^2
6. $4 \times 12 \times 13 \rightarrow 2(48 + 52 + 156)$: 512 cm^2
7. $8 \times 10 \times 15 \rightarrow 2(80 + 120 + 150)$: 700 cm^2
8. $3 \times 4 \times 6 \rightarrow 2(12 + 18 + 24)$: 108 cm^2

Solutions (1 of 7)

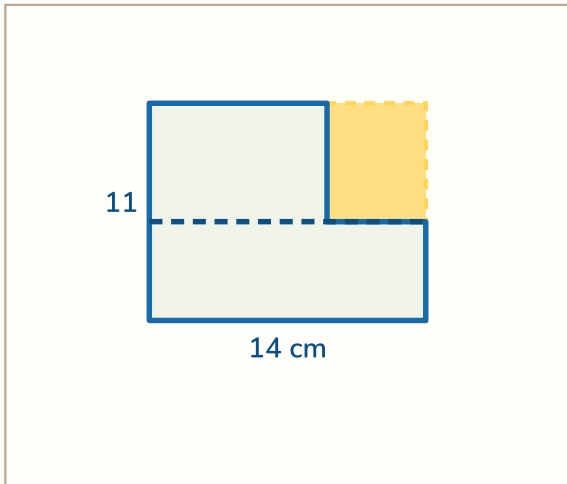
Area of Composite Shapes

Area of composite figures

1.



_____ cm²



First way: pretend the bite was never taken. The whole rectangle would be $14 \times 11 = 154$.

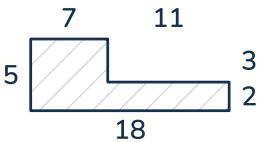
Then take the bite off. It is $5 \times 6 = 30$, so the L is $154 - 30 = 124$ square cm.

Second way, and it works on any of these: cut the L into two rectangles.

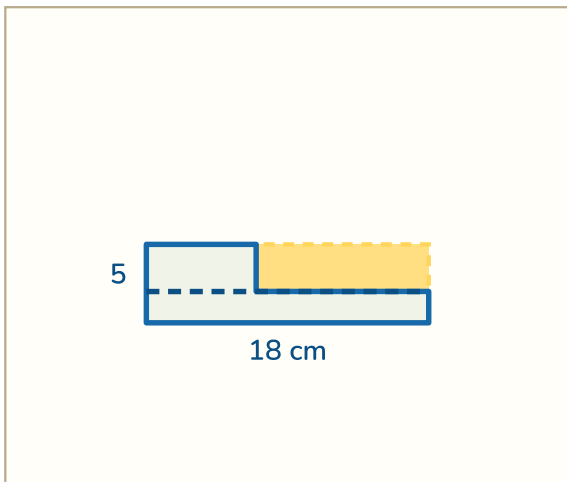
The bottom strip is $14 \times 5 = 70$, and the piece standing on it is $9 \times 6 = 54$.

$70 + 54 = 124$ square cm — the same answer as the first way. Two methods that agree is how you know the answer is right.

2.



_____ cm²



First way: pretend the bite was never taken. The whole rectangle would be $18 \times 5 = 90$.

Then take the bite off. It is $11 \times 3 = 33$, so the L is $90 - 33 = 57$ square cm.

Second way, and it works on any of these: cut the L into two rectangles.

The bottom strip is $18 \times 2 = 36$, and the piece standing on it is $7 \times 3 = 21$.

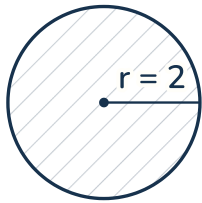
$36 + 21 = 57$ square cm — the same answer as the first way. Two methods that agree is how you know the answer is right.

Solutions (2 of 7)

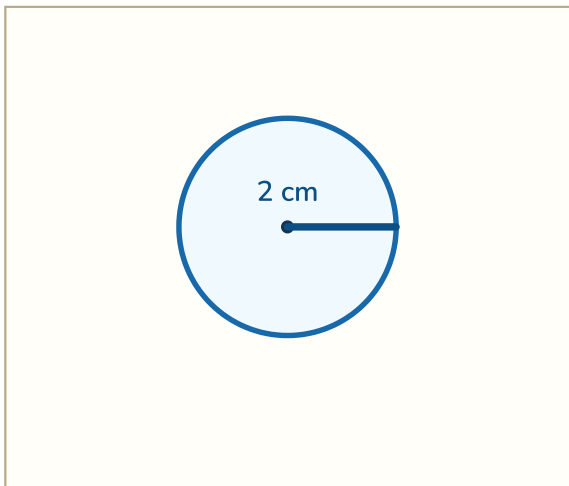
Area of a Circle

Area of a circle

1.



_____ cm^2

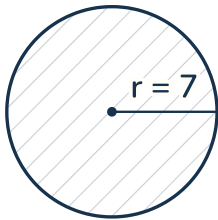


The 2 cm marked here runs from the center to the edge — that is the radius, which is what both formulas want.

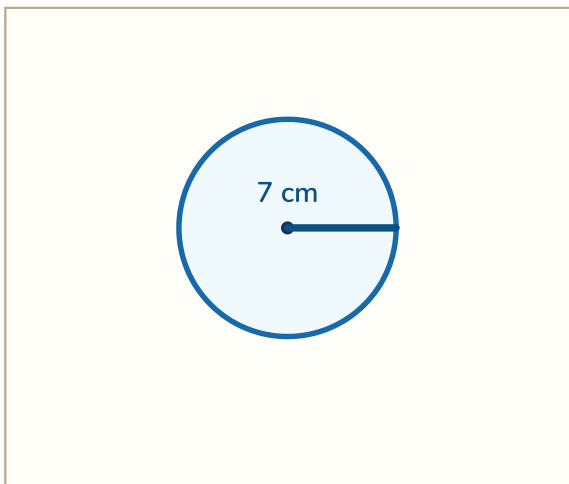
Area is $\pi \times r \times r$. Square the RADIUS first — only the r is squared, not the π with it: $2 \times 2 = 4$.

Then multiply by π : $4 \times 3.14 = 12.56$ square cm.

2.



_____ cm^2



The 7 cm marked here runs from the center to the edge — that is the radius, which is what both formulas want.

Area is $\pi \times r \times r$. Square the RADIUS first — only the r is squared, not the π with it: $7 \times 7 = 49$.

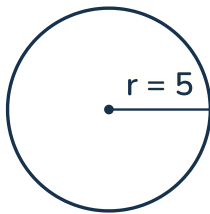
Then multiply by π : $49 \times 3.14 = 153.86$ square cm.

Solutions (3 of 7)

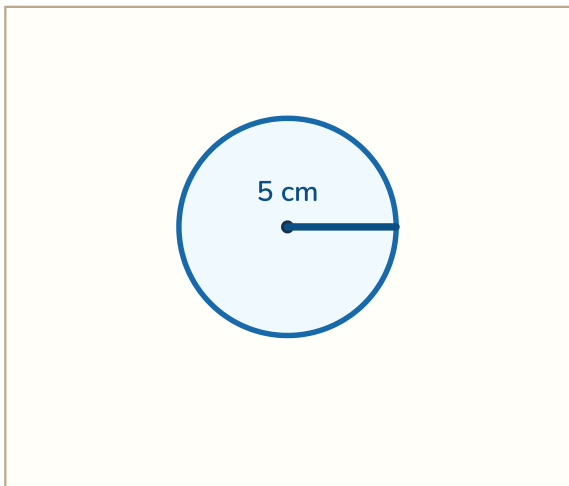
Circumference

Circumference of a circle

1.



_____ cm

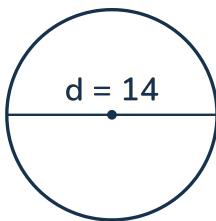


The 5 cm marked here runs from the center to the edge — that is the radius, which is what both formulas want.

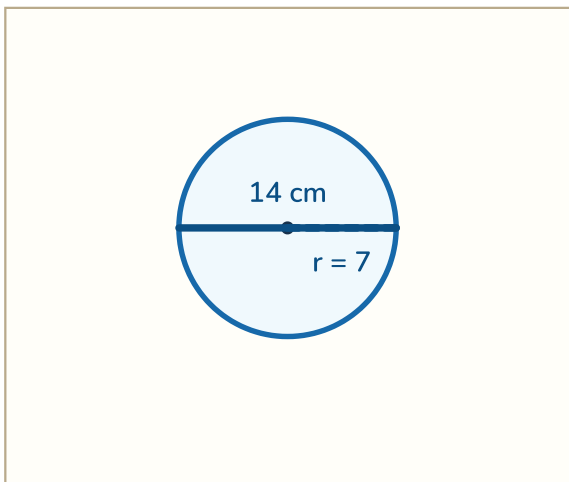
Circumference is $\pi \times$ the whole way across, and the whole way across is two radiuses: $2 \times 5 = 10$.

Then multiply by π : $10 \times 3.14 = 31.4\text{ cm}$. Slightly more than three times across — which is what π has always been.

2.



_____ cm



The 14 cm marked here goes right ACROSS the circle — it is the diameter, the whole way across, which is exactly what a circumference needs.

Circumference is $\pi \times$ the whole way across — that is the diameter, 14.

Then multiply by π : $14 \times 3.14 = 43.96\text{ cm}$. Slightly more than three times across — which is what π has always been.

Solutions (4 of 7)

Angle Pairs

Missing angles in a pair

1.



— degrees

$$83^\circ + x = 180^\circ$$

$$180 - 83 = 97^\circ$$

$$83^\circ + 97^\circ = 180^\circ$$

from the picture, not the numbers

lines crossing:

$x = \text{the angle opposite}$

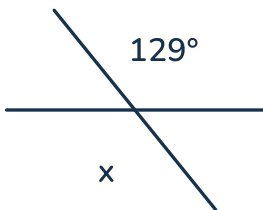
The two angles sit on a STRAIGHT LINE. A straight line is a half turn, which is 180 — not 90, and the picture is the only thing that tells you which.

So the two must add to 180: $x = 180 - 83 = 97^\circ$.

If it had been the other kind you would have taken it from 90 instead and been 90° out — which is why the picture is read first.

One more shape to know: where two straight lines CROSS, the two angles facing each other are equal — nothing is taken away at all. Subtracting there would be wrong.

2.



— degrees

$$\begin{array}{l} 129^\circ \text{ and } x \\ \text{opposite} = \text{equal} \\ 129^\circ \rightarrow 129^\circ \end{array}$$

Two straight lines crossing. This is the pair that is NOT a subtraction — nothing adds to 90 or 180 here, so reaching for either is the mistake.

Angles opposite each other at a crossing are EQUAL. Each one is what is left when the same straight line is taken away from the same straight line, so they cannot differ.

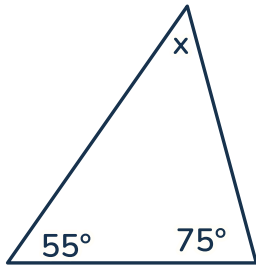
So x is 129° — the same as the one across from it, not 180 minus it.

Solutions (5 of 7)

Angles in a Triangle

The third angle of a triangle

1.



— degrees

$$55 + 75 = 130$$

$$180 - 130 = 50^\circ$$

Every triangle's three angles add to 180 — and that is not a number to take on trust. Tear the three corners off any triangle you like and they fit together into a straight line, every time.

Two of them are given: 55 and 75, which is 130 between them.

So the third takes up what is left of the 180: $180 - 130 = 50^\circ$.

2.



— degrees

$$25 + 60 = 85$$

$$180 - 85 = 95^\circ$$

Every triangle's three angles add to 180 — and that is not a number to take on trust. Tear the three corners off any triangle you like and they fit together into a straight line, every time.

Two of them are given: 25 and 60, which is 85 between them.

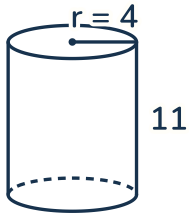
So the third takes up what is left of the 180: $180 - 85 = 95^\circ$.

Solutions (6 of 7)

Volume of Cylinders

Volume of a cylinder

1.



base: 50.24

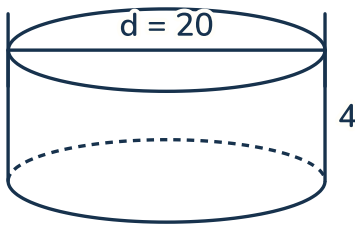
$$50.24 \times 11 = \mathbf{552.64}$$

Same idea as a box: the area of the base times how tall it is. Here the base is a circle, and that is the only difference.

The circle's area is $\pi \times r \times r = 3.14 \times 4 \times 4 = 50.24$ square cm.

Times the height: $50.24 \times 11 = 552.64$ cubic cm.

2.



base: 314

$$314 \times 4 = \mathbf{1256}$$

The 20 cm goes right across, so it is the diameter. Halve it first: the radius is 10. Every one of these formulas SQUARES the radius, so getting this wrong is out by a factor of four, not two.

Same idea as a box: the area of the base times how tall it is. Here the base is a circle, and that is the only difference.

The circle's area is $\pi \times r \times r = 3.14 \times 10 \times 10 = 314$ square cm.

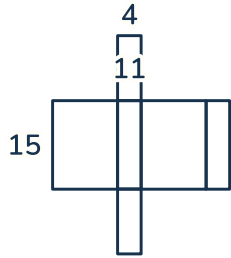
Times the height: $314 \times 4 = 1256$ cubic cm.

Solutions (7 of 7)

Surface Area

Surface area of a box

1.



_____ cm²

front and back: $2 \times 4 \times 15 = 120$

the two sides: $2 \times 11 \times 15 = 330$

top and bottom: $2 \times 4 \times 11 = 88$

total: **538**

A net lays all six faces out flat, so none of them is hidden — which is the whole reason a net is easier than the solid. They still come in three PAIRS.

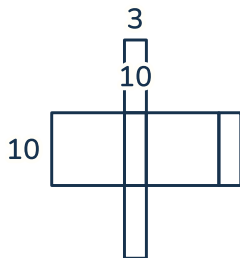
Front and back are 4 by 15, and they are identical — so that pair is $2 \times 4 \times 15 = 120$.

The two sides are 11 by 15, and they are identical — so that pair is $2 \times 11 \times 15 = 330$.

Top and bottom are 4 by 11, and they are identical — so that pair is $2 \times 4 \times 11 = 88$.

Three pairs, six faces, none missed: $120 + 330 + 88 = 538$ square cm.

2.



_____ cm²

front and back: $2 \times 3 \times 10 = 60$

the two sides: $2 \times 10 \times 10 = 200$

top and bottom: $2 \times 3 \times 10 = 60$

total: **320**

A net lays all six faces out flat, so none of them is hidden — which is the whole reason a net is easier than the solid. They still come in three PAIRS.

Front and back are 3 by 10, and they are identical — so that pair is $2 \times 3 \times 10 = 60$.

The two sides are 10 by 10, and they are identical — so that pair is $2 \times 10 \times 10 = 200$.

Top and bottom are 3 by 10, and they are identical — so that pair is $2 \times 3 \times 10 = 60$.

Three pairs, six faces, none missed: $60 + 200 + 60 = 320$ square cm.